

## LOCATION METHOD FOR MOBILE NETWORKS

### Field of the invention

[01] The present invention relates generally to location techniques. More  
5 specifically, the present invention relates to determination of the geographical location of a mobile (i.e. a mobile terminal) within a mobile network.

### Background of the invention

[02] There are two major reasons that have given motivation and fueled the  
10 development of location determining techniques in mobile networks. First, different authorities set requirements for the location determination of mobile terminals. It is highly desirable that certain authorities, such as emergency call centers, can locate the calling party as accurately as possible. In many countries legislation sets requirements for such location methods. For example, in  
15 the USA mobile location to an accuracy of 50 meters for 67 percent of calls and 150 meters for 95 percent of calls will be mandatory in the near future for handset-based solutions. Second, many of the future services provided in mobile networks will be such that they require information about the current geographical location of the mobile terminal.

20 [03] The greater the accuracy of a location method, the better it can serve the application utilizing the location information. This applies especially to densely built urban areas where long-range visibility is not possible. The accuracy of the location methods is dependent on many different factors, such as radio propagation effects. This is a major reason why dense urban areas form  
25 a difficult and challenging environment in terms of location accuracy, with severe multipath characteristics and signal propagating with less attenuation along street canyons than through buildings.

[04] When a mobile is located, successive measurement results are obtained  
from the network. The measurement results are typically not received as co-  
30 ordinates but as parameters which define a certain area within which the mobile is located with a certain probability. As the network normally provides

several parameters for a single measurement, the parameters relating to a single measurement are in this context denoted as a parameter set. On the basis of the parameter set, geometrical limitations can be determined which define the geographical boundaries of one or more areas where the mobile is most likely located. As discussed below, the determination of the location in current cellular networks is widely based on a parameter set including the cell ID and the Timing Advance value, which indicate how far from a certain base station the mobile most probably is located.

**[05]** The current location methods employ the parameter sets obtained by first defining the said one or more areas and then calculating an estimate for the location of the mobile. History data, i.e. previous estimates, can then be used to make the current estimate more accurate. One known method, which is based on a least squares scheme, determines a path for which the sum of the squares of the deviations from the estimated location points obtains a minimum value.

**[06]** A major drawback of the current methods is that they do not preserve the original data revealed by the parameters obtained from the mobile network as to the geographical distribution of the location of the mobile. Instead, with current methods the estimation process moves in an early phase to a point-based approach where the information concerning the geographical distribution is reduced to estimated location points and the final estimate is calculated on the basis of these points. Once the process moves from the geometrical data to point-based information, it can no longer regain the information about the geographical distribution of the location which was included in the parameter sets received from the mobile network.

**[07]** The objective of the invention is to eliminate the drawback described above and to bring about a solution which enables the accurate location of the mobile through efficient usage of the information obtained from the mobile network.

### Summary of the Invention

[08] An objective of the present invention is to find a solution to improve the accuracy of the current location methods. Furthermore, the objective is to achieve a solution not requiring extensive prior labor for achieving the improved accuracy, such as field measurements or data collection.

[09] The invention utilizes location-dependent parameters available from a mobile network for determining the location of the mobile terminal. As mentioned above, the parameters relating to a single measurement are in this context denoted as a parameter set. These parameters indicate the geographical areas within which the mobile most probably is located, i.e. how the location of the mobile is geographically distributed over the area of the system.

[10] In order to improve the accuracy of the system, the invention utilizes the geographical information provided by the parameter sets by forming matrices which indicate the probability distribution of the location of the mobile. A matrix is formed for a parameter set received from the mobile network. Each element of the matrix corresponds to a certain geographical area and contains a value which indicates the probability that the respective mobile is within the said area. At least one matrix formed for a mobile is stored as history data to be used in connection with a subsequent parameter set received for the mobile. When such a parameter set is received, the matrix corresponding to the current parameter set is formed or retrieved, and the elements of the matrix stored earlier are updated. In the updating process the effect of the movement of the mobile on the matrix elements is taken into account, the movement being the estimated movement occurring between the measuring events corresponding to the respective parameter sets. The location estimate is then determined on the basis of the element values of the matrix corresponding to the current parameter set and the element values of the matrix with the updated values.

- 5 [11] Thus the invention utilizes history data in the form of at least one previously formed matrix, which is updated according to the estimated movement of the mobile. By employing the matrices, the original data received from the mobile network on the geographical distribution of the location of the mobile can be retained. The accuracy of the system can hereby be improved by processing the current matrix by one or more previous matrices associated with the mobile in question.
- 10 [12] In one preferred embodiment of the invention, map information is employed in determining the element values of the current matrix. The map information preferably includes information about the type of surface in the geographical area related to an element. The description can be simple, such as road, forest, river, etc. The element values of the current matrix are then weighted according to the type of surface in question.
- 15 [13] In another preferred embodiment map information is employed in updating the element values of the matrix formed in connection with a previous parameter set.
- 20 [14] In addition to the improved accuracy of the system, a further advantage of the invention is that it does not require any special mechanism or laborious steps for forming the matrices. The matrices can be formed "on-the-fly" based on the parameter set received, or they can be formed in advance and stored in a database. In the latter case the parameter set received is used as a search key for retrieving the correct matrix from the database.
- 25 [15] A still further advantage of the invention is that it is not dependent on the network implementation but can be applied to any network where at least one parameter dependent on the location of the mobile is available enabling a matrix to be formed. The method can therefore be used on top of network implementations based on different location-dependent parameters.

#### **Brief Description of the Drawings**

[16] In the following, the invention and its preferred embodiments are described more closely with reference to the examples shown in Figures 1 to 9 in the accompanying drawings, wherein:

- FIG. 1 illustrates the location-dependent information available from a typical cellular network utilizing omni cells,
- FIG. 2 illustrates the location-dependent information available from a typical cellular network utilizing sectored cells,
- FIG. 3 illustrates a preferred embodiment of a system in accordance with the present invention,
- FIG. 4 illustrates a sample matrix formed on the basis of a parameter set received from the mobile network,
- FIG. 5 is an example of a flow diagram illustrating the method of the invention,
- FIG. 6 is an example flow diagram illustrating the processing of a preceding matrix,
- FIG. 7 illustrates how the matrix of FIG. 4 is changed when it is updated once, assuming that all directions of mobile movement are equally probable,
- FIG. 8 illustrates how the matrix of FIG. 4 is changed when it is updated once, assuming that the mobile is traveling directly eastwards, and
- FIG. 9 illustrates one way of forming the matrix which corresponds to a parameter set received.

#### **Detailed Description of the Invention**

- [17] As mentioned above, the method of the invention applies to various kinds of location-dependent information. Depending on the particular cellular system, the location-dependent information provided by the network can be signal strength or signal delay, for example. The determination of the location in current cellular networks is widely based on the Timing Advance value, because the Timing Advance value is directly available from the network. Therefore, Timing Advance is in this context used as an example of the location-dependent signal information available from the mobile network for location determination.

[18] As is known, Timing Advance indicates how far the mobile most probably is from the base station. FIG. 1 illustrates the location dependent information provided by a network with omni-directional base station antennas, whereas FIG. 2 illustrates the same in connection with sectorized cell sites. The network typically provides the Timing Advance information as the minimum and maximum distance from the antenna ( $R_{\min}$  and  $R_{\max}$ ), in which case the mobile terminal is with a certain probability between these limits, i.e. the hatched area A in the figures forms the Timing Advance zone defined by said limits. In addition to the Timing Advance information, the network provides the cell identifier CID, which identifies the cell in which the mobile terminal is located. This information can be given as the coordinates of the cell site. The network further provides an identifier for identifying the mobile in question from among the other mobiles and a time stamp indicating the moment of location measurement. In the case of a sectorized cell, the network also provides the sector information. Thus for each location determination the network provides a parameter set which commonly includes the following information: cell identifying data, such as the coordinates of the Base Transceiver Station, Timing Advance information, such as  $R_{\max}$  and  $R_{\min}$ , an identifier for identifying the mobile in question from among the other mobiles, a time stamp indicating the moment of the location measurement, and possibly the sector information.

[19] FIG. 3 illustrates the key elements of the system according to the present invention. It is assumed here that the mobile network is a GSM Public Land Mobile Network. Communication between the network and a mobile terminal MS in a cell takes place via a radio path by way of a Base Transceiver Station (BTS) 31. The Base Transceiver Stations are connected to Base Station Controllers (BSC) 32. Several Base Transceiver Stations are usually under the control of one BSC, and several Base Station Controllers are connected to one Mobile Switching Centre (MSC) 33, which carries out the main switching functions of the mobile network. In addition, the MSC connects the mobile network with external networks. For positioning purposes, the MSC is connected to a

Gateway Mobile Location Center (GMLC) 34, which collects mobile positioning information in a positioning database 35. As mentioned above, it is assumed in this context that the GMLC supports Cell ID and Timing Advance. This means that for each location determination the GMLC provides a parameter set, including the parameters discussed above in connection with FIG. 1 and 2.

[20] The parameter sets available from the mobile network are processed in an accuracy server 38, which receives location requests from external objects, such as service applications residing in the network to which the accuracy server is connected. In order to be able to determine a location estimate on the basis of a parameter set received, the accuracy server forms a matrix on the basis of the parameter set or retrieves a matrix corresponding to the parameter set from among a plurality of matrices formed in advance and stored in a matrix database 39a. The accuracy server further uses mobile-specific history data stored in a history database 39b. This data comprises matrices obtained in connection with the parameter sets received earlier for the mobile in question. The content of these matrices is discussed below. In determining the element values of the matrices, the accuracy server preferably further employs map information stored in a map database 39c, although the use of map information is not necessary. The same applies to the use of in-advance calculated matrices, i.e. the matrix database is not necessary, but the matrix corresponding to the current parameter set can be calculated in real-time.

[21] The information required by the accuracy server for processing the parameter sets can also be stored in a single database. The information is preferably stored in connection with the accuracy server, although it can be distributed in the network to which the accuracy server is connected.

[22] Upon receiving a parameter set, the accuracy server calculates a matrix corresponding to this parameter set. On the other hand, if the matrices have been calculated in advance, the accuracy server retrieves said matrix from the

database 39a, and the parameter set is used as a search key for finding the correct matrix. The matrix contains  $n \times n$  elements, each covering a certain geographical area and each including a value indicating a probability that the mobile is within the area covered by the element. FIG. 4 shows an example of a matrix comprising  $10 \times 10$  elements. In practice, the number of elements is much greater, e.g.  $40 \times 40$  elements. Each element corresponds to a coordinate pair  $X_i/Y_i$  ( $i=0 \dots 9$ ), which defines the geographical area covered by the element. In practice, the size of each element can be  $25 \times 25$  m, for example, in which case a  $40 \times 40$  matrix would cover an area of one square kilometer. In the example of Fig. 4, the element values are given as percents. The elements covered by the Timing Advance zone are given the value of 100, while the other elements are given the value of zero.

[23] FIG. 5 illustrates the estimation process performed by the accuracy server. As mentioned above, upon receiving a parameter set the accuracy server calculates a matrix corresponding to this parameter set or retrieves said matrix from the database 39a using the parameter set as a search key (step 51). The parameter sets can go through a normalization process so that the parameter sets which equal one another with a given accuracy are mapped to the same matrix. If the accuracy server retrieves the matrix, the matrices are preferably formed using a suitable calibration mechanism, such as the GPS system. In other words, when the matrices are formed before the commissioning of the system, the distribution of the location of the mobile is determined by the calibration mechanism and the matrix is formed on the basis of the results given by the calibration mechanism. A combinatory mechanism can also be used, for example, so that the matrices calculated in advance are further processed in the accuracy server in order to obtain the final matrix describing the probability distribution. In a preferred embodiment of the invention, this is done by using map information to adjust the element values of the matrix.



[24] In this embodiment the accuracy server retrieves map information in order to weight the element values by this data. The matrices to be weighted can originate from a database or can be formed in real-time by the accuracy server. Map information refers here to any information which correlates with the location probability or with the movement probability of the mobile. The map information used by the accuracy server is preferably in the form of map matrices similar to the matrices formed on the basis of the parameter sets, except that in the map matrices an individual element indicates the type of the surface covered by the element. The classification into surface types can be simple, such as road, forest, river, etc., each type being assigned a weight value. Some types are stronger than others; for instance, if a road goes through a forest, the subscriber is more likely traveling along the road rather than through the forest, so the type of the element is set to "road". The map matrix can be formed in real-time from the information retrieved from the map database, or the information in the database can be in the form of matrices.

[25] The element values of the matrix formed on the basis of the parameter set received are then weighted according to the type of land in question (step 53), whereby a weighted matrix is obtained. A previous matrix obtained in connection with a preceding parameter set relating to the same mobile is also retrieved from the history database 39b, and this matrix is supplied to an update process. In this context, the previous matrix is also called the history matrix. In the update process (step 54) the effect of the estimated movement of the mobile on the location distribution is taken into account by spreading the probability distribution of the previous matrix according to the movement data. This operation is based on the information available about the movement of the mobile, such as speed and/or direction information. Map correlation coupled with movement information can be used to yield more accurate results. If no information on the movement is available, the probability distribution is spread evenly in all directions. As a result of the update process, a spread history matrix is obtained.

[26] The current matrix and the spread history matrix are supplied to a combination process where a combined matrix of the same size is determined according to predetermined rules (step 55). At least one location estimate is then calculated on the basis of the combined matrix (step 56). Furthermore, the combined matrix is supplied to the history database, where it replaces the previous matrix, i.e. the next time the previous matrix is retrieved, the combined matrix calculated in connection with the then preceding parameter set is obtained as the previous matrix to be updated.

[27] FIG. 6 illustrates the updating of the previous matrix, in which the values of the previous matrix are updated according to the assumed movement of the mobile. The update process includes one or more calculation rounds. During each round the probability distribution carried by the history matrix is spread once. The process employs three parameters which define how many rounds are needed each time; n, T, and T1, where n indicates the number of times the spreading has been performed, T indicates the time elapsed from the previous update process (i.e. the time elapsed since the location of the mobile was estimated previously), and T1 is a fixed time interval which is deducted from T every time the matrix is spread.

[28] The process first forms  $n1 \times n1$  basic coefficients  $w_{i,j}$  used in the spreading process (step 60). In this example  $n1=3$  and all the coefficients get the value of 1 as follows:

$$W = \begin{bmatrix} w_{i-1,j-1} & w_{i,j-1} & w_{i+1,j-1} \\ w_{i-1,j} & w_{i,j} & w_{i+1,j} \\ w_{i-1,j+1} & w_{i,j+1} & w_{i+1,j+1} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}.$$

[29] Parameter n is then given the value of zero (step 61), since no spreading has yet taken place, and the value of T1 is deducted from the value of T (step 62).

[30] The basic coefficients are then adjusted according to the movement information relating to the mobile, such as the direction and speed information (step 63). Map information can also be utilized in determining the adjusted

coefficients. It is assumed in this example that the mobile is moving directly eastwards, whereby the adjusted coefficients  $w'_{i,j}$  are as follows:

$$W' = \begin{bmatrix} w'_{i-1,j-1} & w'_{i,j-1} & w'_{i+1,j-1} \\ w'_{i-1,j} & w'_{i,j} & w'_{i+1,j} \\ w'_{i-1,j+1} & w'_{i,j+1} & w'_{i+1,j+1} \end{bmatrix} = \begin{bmatrix} 1 & 1 & 0 \\ 1 & 1 & 0 \\ 1 & 1 & 0 \end{bmatrix}.$$

- [31] In a spreading process the adjusted coefficients are then used to adjust  
5 the value of each element  $e_{k,l}$  of the history matrix as follows (step 64):

$$E_{k,l} = \frac{\sum_{k=i-1}^{i+1} \sum_{l=j-1}^{j+1} w'_{k,l} \times e_{k,l}}{M}$$

- where M is the sum of adjusted coefficients deviating from zero, and  $E_{k,l}$  is the element value of the spread matrix. Thus the spread matrix is obtained so that each element of the previous matrix is replaced by a weighted  
10 average of itself and those of its neighbors which do not get a zero weight. In practice the number of elements affecting the adjusted value of each element can be greater, for example 16 (4×4 weights) or 25 (5×5 weights).

- [32] After the first spreading round, the accuracy server tests whether T is still greater than zero and n smaller than a predefined limit  $n_{\max}$  (step 65). If  
15 this is the case, the above-described spreading steps 63 and 64 are repeated. At the beginning of each new round, the value of n is incremented by one (step 66), and the value of T1 is deducted from the current value of T (step 62). A new matrix is calculated as long as T remains greater than zero, and n smaller than a predefined limit  $n_{\max}$ .

- 20 [33] As to step 63, it is further to be noted that the adjustment of the basic coefficients by means of the movement information may be performed only once for each update process (i.e once for each step 54). The adjustment according to the map information has to be made separately for each matrix element during each spreading round, since the map information used to adjust  
25 the coefficients is element-specific, i.e. depends on the area defined by the element.

[34] FIG. 7 illustrates how the matrix of FIG. 4 has changed after one spreading round when the above basic coefficients are used. Thus in this case no direction-based weighting is employed, but it is assumed that all directions are equally probable. As can be seen from the figure, the probability distribution has spread; the number of elements having a non-zero value has increased from 17 to 45.

[35] FIG. 8 illustrates how the matrix of FIG. 4 has changed after one spreading round when the above-described adjusted coefficients are used. Thus, in this case it is assumed that the mobile is traveling eastwards. Now the number of elements having a non-zero value has increased to 37. Utilizing the map information in the spreading process means that the probabilities spread faster along roads than along forests, for example.

[36] The spread history matrix and the current matrix can be combined in various ways. However, there are always two probability values, A and B, corresponding to a certain area, one from the element corresponding to the respective area in the current matrix and another from the element corresponding to the respective area in the spread matrix. In the combination process (step 55), a new element value is determined for the respective element of the combined matrix based on these two values. There are at least three possible ways to determine the new element value for each element of the combined matrix:

1. calculate the sum of the two values, i.e.  $A+B$ ,
2. calculate a weighted sum of the two values, i.e.  $r \times A + (1-r) \times B$ ,
3. select the value which is the highest one, i.e.  $\max\{A, B\}$ .

As mentioned above, the combined matrix formed in one of the above ways is stored as a new history matrix.

[37] Based on the values of the combined matrix, the final estimate(s) can also be determined in various ways. At least the following ways are possible:

1. The coordinates of the element containing the highest value are selected as the location estimate.

2. The coordinates corresponding to the center of gravity of the element values are selected as the location estimate. The center of gravity here refers to an average (calculated in a desired way) of the coordinate values associated with the element values.

5           3. A certain area, which is obtained based on the previous estimate and the speed and/or direction information, is examined. The element containing the highest value within that area is then selected as the location estimate. Another alternative is to select as the location estimate the coordinates corresponding to the center of gravity of the element values of the area.

10           4. Local averages can be calculated for element groups of the desired size. For example, averages can be computed over local areas of  $100 \times 100 \text{ m}^2$ , and the center point of the local area having the highest average can be selected as the local estimate. The form of the local area can also be other than a square, for example a circle.

15           5. Areas of predetermined form, such as circles, are drawn around estimate candidates, each area covering a certain proportion of the total sum of the elements. The candidate is then selected for which the said area is the smallest.

[38]   The best alternative can be selected by testing the system in the desired  
20   environment and finding the alternative yielding the best results.

[39]   The formation of the matrix corresponding to the current parameter set  
(step 51) is discussed next. As mentioned above, the matrix can be formed  
directly in real-time on the basis of the parameter set, or it can be retrieved  
from among the matrices produced in advance by using the parameter set as  
25   a search key. A third alternative is to use a combination of these two methods.

[40]   When the matrix is formed in real-time from the parameter set, the geometrical counterpart of the parameter set, i.e. the area defined by the parameter set, can be superimposed on an empty matrix covering the area in question. FIG. 9 illustrates this by showing a Timing Advance zone 90 superimposed on a  $7 \times 7$  matrix.. Elements are then assigned values which reflect correspondence between area represented by the element, and the area that is actually covered by the parameter set. Thus for example, Fig. 9 the shape 90 represents the geometrical area indicated by the parameter set. In the case of

element 93 only about 40% of the element area is covered by shape 90, and thus the element is assigned the value 4, while element 95 is covered by shape 90 to about 70% of its area, and thus is given the value 7. As the matrix values range from one (no coverage) to ten (full coverage), these values can then be adjusted employing the map information. Alternatively, all the elements overlapping the geometric counterpart can be assigned the value of one, while the rest of the elements, which do not overlap with the geometrical counterpart, are assigned the value of zero.

[41] When the matrix is retrieved from a database containing matrices formed in advance, it is preferable to measure the actual probability distribution by means of a suitable mechanism, such as the GPS. Thus, in this case the matrix elements indicate the probability distribution measured in advance in real environment. The parameter sets which are substantially equal to each other, i.e. which with a desired accuracy have the same parameter values, are associated with the same matrix.

[42] The third alternative which combines the above mechanisms could be such that an in-advance calculated matrix is always used when it is available, while the matrix is computed in real-time only when no calculated matrix is available in advance. This is because a matrix determined in-advance probably represents a more reliable perception of the probability distribution.

[43] Although the invention was described above with reference to the examples shown in the appended drawings, it is obvious that the invention is not limited to these, but may be modified by those skilled in the art without departing from the scope and spirit of the invention. In a simplified form of the invention, no map information or direction information is used, i.e. the probability distribution is spread evenly in all directions. More than one history matrix can be employed for processing the current matrix. The network elements used can also vary. For example, the parameter sets can be received from any network entity having access to them, and the steps of the method can be distributed among different network elements. In the future a mobile may per-

form some or all of the steps of the method. Depending on the content of the parameter set, a mobile terminal might simply need external information required to form the matrices in order to be able to perform the steps of the method. In a further embodiment, the mobile terminal can download predetermined matrices from the network, i.e. matrix formation is not necessarily  
5 needed in the terminal. Upon receiving a parameter set, the mobile terminal retrieves or downloads from the network an in-advance calculated matrix which corresponds to the parameter set received. In this respect the mobile terminal can thus act similarly as the accuracy server.

10

11  
12  
13  
14  
15  
16  
17  
18  
19  
20  
21  
22  
23  
24  
25  
26  
27  
28  
29  
30  
31  
32  
33  
34  
35  
36  
37  
38  
39  
40  
41  
42  
43  
44  
45  
46  
47  
48  
49  
50  
51  
52  
53  
54  
55  
56  
57  
58  
59  
60  
61  
62  
63  
64  
65  
66  
67  
68  
69  
70  
71  
72  
73  
74  
75  
76  
77  
78  
79  
80  
81  
82  
83  
84  
85  
86  
87  
88  
89  
90  
91  
92  
93  
94  
95  
96  
97  
98  
99  
100  
101  
102  
103  
104  
105  
106  
107  
108  
109  
110  
111  
112  
113  
114  
115  
116  
117  
118  
119  
120  
121  
122  
123  
124  
125  
126  
127  
128  
129  
130  
131  
132  
133  
134  
135  
136  
137  
138  
139  
140  
141  
142  
143  
144  
145  
146  
147  
148  
149  
150  
151  
152  
153  
154  
155  
156  
157  
158  
159  
160  
161  
162  
163  
164  
165  
166  
167  
168  
169  
170  
171  
172  
173  
174  
175  
176  
177  
178  
179  
180  
181  
182  
183  
184  
185  
186  
187  
188  
189  
190  
191  
192  
193  
194  
195  
196  
197  
198  
199  
200  
201  
202  
203  
204  
205  
206  
207  
208  
209  
210  
211  
212  
213  
214  
215  
216  
217  
218  
219  
220  
221  
222  
223  
224  
225  
226  
227  
228  
229  
230  
231  
232  
233  
234  
235  
236  
237  
238  
239  
240  
241  
242  
243  
244  
245  
246  
247  
248  
249  
250  
251  
252  
253  
254  
255  
256  
257  
258  
259  
260  
261  
262  
263  
264  
265  
266  
267  
268  
269  
270  
271  
272  
273  
274  
275  
276  
277  
278  
279  
280  
281  
282  
283  
284  
285  
286  
287  
288  
289  
290  
291  
292  
293  
294  
295  
296  
297  
298  
299  
300  
301  
302  
303  
304  
305  
306  
307  
308  
309  
310  
311  
312  
313  
314  
315  
316  
317  
318  
319  
320  
321  
322  
323  
324  
325  
326  
327  
328  
329  
330  
331  
332  
333  
334  
335  
336  
337  
338  
339  
340  
341  
342  
343  
344  
345  
346  
347  
348  
349  
350  
351  
352  
353  
354  
355  
356  
357  
358  
359  
360  
361  
362  
363  
364  
365  
366  
367  
368  
369  
370  
371  
372  
373  
374  
375  
376  
377  
378  
379  
380  
381  
382  
383  
384  
385  
386  
387  
388  
389  
390  
391  
392  
393  
394  
395  
396  
397  
398  
399  
400  
401  
402  
403  
404  
405  
406  
407  
408  
409  
410  
411  
412  
413  
414  
415  
416  
417  
418  
419  
420  
421  
422  
423  
424  
425  
426  
427  
428  
429  
430  
431  
432  
433  
434  
435  
436  
437  
438  
439  
440  
441  
442  
443  
444  
445  
446  
447  
448  
449  
450  
451  
452  
453  
454  
455  
456  
457  
458  
459  
460  
461  
462  
463  
464  
465  
466  
467  
468  
469  
470  
471  
472  
473  
474  
475  
476  
477  
478  
479  
480  
481  
482  
483  
484  
485  
486  
487  
488  
489  
490  
491  
492  
493  
494  
495  
496  
497  
498  
499  
500  
501  
502  
503  
504  
505  
506  
507  
508  
509  
510  
511  
512  
513  
514  
515  
516  
517  
518  
519  
520  
521  
522  
523  
524  
525  
526  
527  
528  
529  
530  
531  
532  
533  
534  
535  
536  
537  
538  
539  
540  
541  
542  
543  
544  
545  
546  
547  
548  
549  
550  
551  
552  
553  
554  
555  
556  
557  
558  
559  
560  
561  
562  
563  
564  
565  
566  
567  
568  
569  
570  
571  
572  
573  
574  
575  
576  
577  
578  
579  
580  
581  
582  
583  
584  
585  
586  
587  
588  
589  
590  
591  
592  
593  
594  
595  
596  
597  
598  
599  
600  
601  
602  
603  
604  
605  
606  
607  
608  
609  
610  
611  
612  
613  
614  
615  
616  
617  
618  
619  
620  
621  
622  
623  
624  
625  
626  
627  
628  
629  
630  
631  
632  
633  
634  
635  
636  
637  
638  
639  
640  
641  
642  
643  
644  
645  
646  
647  
648  
649  
650  
651  
652  
653  
654  
655  
656  
657  
658  
659  
660  
661  
662  
663  
664  
665  
666  
667  
668  
669  
670  
671  
672  
673  
674  
675  
676  
677  
678  
679  
680  
681  
682  
683  
684  
685  
686  
687  
688  
689  
690  
691  
692  
693  
694  
695  
696  
697  
698  
699  
700  
701  
702  
703  
704  
705  
706  
707  
708  
709  
710  
711  
712  
713  
714  
715  
716  
717  
718  
719  
720  
721  
722  
723  
724  
725  
726  
727  
728  
729  
730  
731  
732  
733  
734  
735  
736  
737  
738  
739  
740  
741  
742  
743  
744  
745  
746  
747  
748  
749  
750  
751  
752  
753  
754  
755  
756  
757  
758  
759  
760  
761  
762  
763  
764  
765  
766  
767  
768  
769  
770  
771  
772  
773  
774  
775  
776  
777  
778  
779  
780  
781  
782  
783  
784  
785  
786  
787  
788  
789  
790  
791  
792  
793  
794  
795  
796  
797  
798  
799  
800  
801  
802  
803  
804  
805  
806  
807  
808  
809  
810  
811  
812  
813  
814  
815  
816  
817  
818  
819  
820  
821  
822  
823  
824  
825  
826  
827  
828  
829  
830  
831  
832  
833  
834  
835  
836  
837  
838  
839  
840  
841  
842  
843  
844  
845  
846  
847  
848  
849  
850  
851  
852  
853  
854  
855  
856  
857  
858  
859  
860  
861  
862  
863  
864  
865  
866  
867  
868  
869  
870  
871  
872  
873  
874  
875  
876  
877  
878  
879  
880  
881  
882  
883  
884  
885  
886  
887  
888  
889  
890  
891  
892  
893  
894  
895  
896  
897  
898  
899  
900  
901  
902  
903  
904  
905  
906  
907  
908  
909  
910  
911  
912  
913  
914  
915  
916  
917  
918  
919  
920  
921  
922  
923  
924  
925  
926  
927  
928  
929  
930  
931  
932  
933  
934  
935  
936  
937  
938  
939  
940  
941  
942  
943  
944  
945  
946  
947  
948  
949  
950  
951  
952  
953  
954  
955  
956  
957  
958  
959  
960  
961  
962  
963  
964  
965  
966  
967  
968  
969  
970  
971  
972  
973  
974  
975  
976  
977  
978  
979  
980  
981  
982  
983  
984  
985  
986  
987  
988  
989  
990  
991  
992  
993  
994  
995  
996  
997  
998  
999  
1000  
1001  
1002  
1003  
1004  
1005  
1006  
1007  
1008  
1009  
1010  
1011  
1012  
1013  
1014  
1015  
1016  
1017  
1018  
1019  
1020  
1021  
1022  
1023  
1024  
1025  
1026  
1027  
1028  
1029  
1030  
1031  
1032  
1033  
1034  
1035  
1036  
1037  
1038  
1039  
1040  
1041  
1042  
1043  
1044  
1045  
1046  
1047  
1048  
1049  
1050  
1051  
1052  
1053  
1054  
1055  
1056  
1057  
1058  
1059  
1060  
1061  
1062  
1063  
1064  
1065  
1066  
1067  
1068  
1069  
1070  
1071  
1072  
1073  
1074  
1075  
1076  
1077  
1078  
1079  
1080  
1081  
1082  
1083  
1084  
1085  
1086  
1087  
1088  
1089  
1090  
1091  
1092  
1093  
1094  
1095  
1096  
1097  
1098  
1099  
1100  
1101  
1102  
1103  
1104  
1105  
1106  
1107  
1108  
1109  
1110  
1111  
1112  
1113  
1114  
1115  
1116  
1117  
1118  
1119  
1120  
1121  
1122  
1123  
1124  
1125  
1126  
1127  
1128  
1129  
1130  
1131  
1132  
1133  
1134  
1135  
1136  
1137  
1138  
1139  
1140  
1141  
1142  
1143  
1144  
1145  
1146  
1147  
1148  
1149  
1150  
1151  
1152  
1153  
1154  
1155  
1156  
1157  
1158  
1159  
1160  
1161  
1162  
1163  
1164  
1165  
1166  
1167  
1168  
1169  
1170  
1171  
1172  
1173  
1174  
1175  
1176  
1177  
1178  
1179  
1180  
1181  
1182  
1183  
1184  
1185  
1186  
1187  
1188  
1189  
1190  
1191  
1192  
1193  
1194  
1195  
1196  
1197  
1198  
1199  
1200  
1201  
1202  
1203  
1204  
1205  
1206  
1207  
1208  
1209  
1210  
1211  
1212  
1213  
1214  
1215  
1216  
1217  
1218  
1219  
1220  
1221  
1222  
1223  
1224  
1225  
1226  
1227  
1228  
1229  
1230  
1231  
1232  
1233  
1234  
1235  
1236  
1237  
1238  
1239  
1240  
1241  
1242  
1243  
1244  
1245  
1246  
1247  
1248  
1249  
1250  
1251  
1252  
1253  
1254  
1255  
1256  
1257  
1258  
1259  
1260  
1261  
1262  
1263  
1264  
1265  
1266  
1267  
1268  
1269  
1270  
1271  
1272  
1273  
1274  
1275  
1276  
1277  
1278  
1279  
1280  
1281  
1282  
1283  
1284  
1285  
1286  
1287  
1288  
1289  
1290  
1291  
1292  
1293  
1294  
1295  
1296  
1297  
1298  
1299  
1300  
1301  
1302  
1303  
1304  
1305  
1306  
1307  
1308  
1309  
1310  
1311  
1312  
1313  
1314  
1315  
1316  
1317  
1318  
1319  
1320  
1321  
1322  
1323  
1324  
1325  
1326  
1327  
1328  
1329  
1330  
1331  
1332  
1333  
1334  
1335  
1336  
1337  
1338  
1339  
1340  
1341  
1342  
1343  
1344  
1345  
1346  
1347  
1348  
1349  
1350  
1351  
1352  
1353  
1354  
1355  
1356  
1357  
1358  
1359  
1360  
1361  
1362  
1363  
1364  
1365  
1366  
1367  
1368  
1369  
1370  
1371  
1372  
1373  
1374  
1375  
1376  
1377  
1378  
1379  
1380  
1381  
1382  
1383  
1384  
1385  
1386  
1387  
1388  
1389  
1390  
1391  
1392  
1393  
1394  
1395  
1396  
1397  
1398  
1399  
1400  
1401  
1402  
1403  
1404  
1405  
1406  
1407  
1408  
1409  
1410  
1411  
1412  
1413  
1414  
1415  
1416  
1417  
1418  
1419  
1420  
1421  
1422  
1423  
1424  
1425  
1426  
1427  
1428  
1429  
1430  
1431  
1432  
1433  
1434  
1435  
1436  
1437  
1438  
1439  
1440  
1441  
1442  
1443  
1444  
1445  
1446  
1447  
1448  
1449  
1450  
1451  
1452  
1453  
1454  
1455  
1456  
1457  
1458  
1459  
1460  
1461  
1462  
1463  
1464  
1465  
1466  
1467  
1468  
1469  
1470  
1471  
1472  
1473  
1474  
1475  
1476  
1477  
1478  
1479  
1480  
1481  
1482  
1483  
1484  
1485  
1486  
1487  
1488  
1489  
1490  
1491  
1492  
1493  
1494  
1495  
1496  
1497  
1498  
1499  
1500  
1501  
1502  
1503  
1504  
1505  
1506  
1507  
1508  
1509  
1510  
1511  
1512  
1513  
1514  
1515  
1516  
1517  
1518  
1519  
1520  
1521  
1522  
1523  
1524  
1525  
1526  
1527  
1528  
1529  
1530  
1531  
1532  
1533  
1534  
1535  
1536  
1537  
1538  
1539  
1540  
1541  
1542  
1543  
1544  
1545  
1546  
1547  
1548  
1549  
1550  
1551  
1552  
1553  
1554  
1555  
1556  
1557  
1558  
1559  
1560  
1561  
1562  
1563  
1564  
1565  
1566  
1567  
1568  
1569  
1570  
1571  
1572  
1573  
1574  
1575  
1576  
1577  
1578  
1579  
1580  
1581  
1582  
1583  
1584  
1585  
1586  
1587  
1588  
1589  
1590  
1591  
1592  
1593  
1594  
1595  
1596  
1597  
1598  
1599  
1600  
1601  
1602  
1603  
1604  
1605  
1606  
1607  
1608  
1609  
1610  
1611  
1612  
1613  
1614  
1615  
1616  
1617  
1618  
1619  
1620  
1621  
1622  
1623  
1624  
1625  
1626  
1627  
1628  
1629  
1630  
1631  
1632  
1633  
1634  
1635  
1636  
1637  
1638  
1639  
1640  
1641  
1642  
1643  
1644  
1645  
1646  
1647  
1648  
1649  
1650  
1651  
1652  
1653  
1654  
1655  
1656  
1657  
1658  
1659  
1660  
1661  
1662  
1663  
1664  
1665  
1666  
1667  
1668  
1669  
1670  
1671  
1672  
1673  
1674  
1675  
1676  
1677  
1678  
1679  
1680  
1681  
1682  
1683  
1684  
1685  
1686  
1687  
1688  
1689  
1690  
1691  
1692  
1693  
1694  
1695  
1696  
1697  
1698  
1699  
1700  
1701  
1702  
1703  
1704  
1705  
1706  
1707  
1708  
1709  
1710  
1711  
1712  
1713  
1714  
1715  
1716  
1717  
1718  
1719  
1720  
1721  
1722  
1723  
1724  
1725  
1726  
1727  
1728  
1729  
1730  
1731  
1732  
1733  
1734  
1735  
1736  
1737  
1738  
1739  
1740  
1741  
1742  
1743  
1744  
1745  
1746  
1747  
1748  
1749  
1750  
1751  
1752  
1753  
1754  
1755  
1756  
1757  
1758  
1759  
1760  
1761  
1762  
1763  
1764  
1765  
1766  
1767  
1768  
1769  
1770  
1771  
1772  
1773  
1774  
1775  
1776  
1777  
1778  
1779  
1780  
1781  
1782  
1783  
1784  
1785  
1786  
1787  
1788  
1789  
1790  
1791  
1792  
1793  
1794  
1795  
1796  
1797  
1798  
1799  
1800  
1801  
1802  
1803  
1804  
1805  
1806  
1807  
1808  
1809  
1810  
1811  
1812  
1813  
1814  
1815  
1816  
1817  
1818  
1819  
1820  
1821  
1822  
1823  
1824  
1825  
1826  
1827  
1828  
1829  
1830  
1831  
1832  
1833  
1834  
1835  
1836  
1837  
1838  
1839  
1840  
1841  
1842  
1843  
1844  
1845  
1846  
1847  
1848  
1849  
1850  
1851  
1852  
1853  
1854  
1855  
1856  
1857  
1858  
1859  
1860  
1861  
1862  
1863  
1864  
1865  
1866  
1867  
1868  
1869  
1870  
1871  
1872  
1873  
1874  
1875  
1876  
1877  
1878  
1879  
1880  
1881  
1882  
1883  
1884  
1885  
1886  
1887  
1888  
1889  
1890  
1891  
1892  
1893  
1894  
1895  
1896  
1897  
1898  
1899  
1900  
1901  
1902  
1903  
1904  
1905  
1906  
1907  
1908  
1909  
1910  
1911  
1912  
1913  
1914  
1915  
1916  
1917  
1918  
1919  
1920  
1921  
1922  
1923  
1924  
1925  
1926  
1927  
1928  
1929  
1930  
1931  
1932  
1933  
1934  
1935  
1936  
1937  
1938  
1939  
1940  
1941  
1942  
1943  
1944  
1945  
1946  
1947  
1948  
1949  
1950  
1951  
1952  
1953  
1954  
1955  
1956  
1957  
1958  
1959  
1960  
1961  
1962  
1963  
1964  
1965  
1966  
1967  
1968  
1969  
1970  
1971  
1972  
1973  
1974  
1975  
1976  
1977  
1978  
1979  
1980  
1981  
1982  
1983  
1984  
1985  
1986  
1987  
1988  
1989  
1990  
1991  
1992  
1993  
1994  
1995  
1996  
1997  
1998  
1999  
2000  
2001  
2002  
2003  
2004  
2005  
2006  
2007  
2008  
2009  
2010  
2011  
2012  
2013  
2014  
2015  
2016  
2017  
2018  
2019  
2020  
2021  
2022  
2023  
2024  
2025  
2026  
2027  
2028  
2029  
2030  
2031  
2032  
2033  
2034  
2035  
2036  
2037  
2038  
2039  
2040  
2041  
2042  
2043  
2044  
2045  
2046  
2047  
2048  
2049  
2050  
2051  
2052  
2053  
2054  
2055  
2056  
2057  
2058  
2059  
2060  
2061  
2062  
2063  
2064  
2065  
2066  
2067  
2068  
2069  
2070  
2071  
2072  
2073  
2074  
2075  
2076  
2077  
2078  
2079  
2080  
2081  
2082  
2083  
2084  
2085  
2086  
2087  
2088  
2089  
2090  
2091  
2092  
2093  
2094  
2095  
2096  
2097  
2098  
2099  
2100  
2101  
2102  
2103  
2104  
2105  
2106  
2107  
2108  
2109  
2110  
2111  
2112  
2113  
2114  
2115  
2116  
2117  
2118  
2119  
2120  
2121  
2122  
2123  
2124  
2125  
2126  
2127  
2128  
2129  
2130  
2131  
2132  
2133  
2134  
2135  
2136  
2137  
2138  
2139  
2140  
2141  
2142  
2143  
2144  
2145  
2146  
2147  
2148  
2149  
2150  
2151  
2152  
2153  
2154  
2155  
2156  
2157  
2158  
2159  
2160  
2161  
2162  
2163  
2164  
2165  
2166  
2167  
2168  
2169  
2170  
2171  
2172  
2173  
2174  
2175  
2176  
2177  
2178  
2179  
2180  
2181  
2182  
2183  
2184  
2185  
2186  
2187  
2188  
2189  
2190  
2191  
2192  
2193  
2194  
2195  
2196  
2197  
2198  
2199  
2200  
2201  
2202  
2203  
2204  
2205  
2206  
2207  
2208  
2209  
2210  
2211  
2212  
2213  
2214  
2215  
2216  
2217  
2218